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The information contained in this Educator Guide is designed to raise educator awareness of the uvtwerwtg qh vjg Pgy [qtm Uvcvg Itcfgu 56: Ocvjgocvkeu Vguvu ogcuwtkpi vjg Pgy [qtm Uvcvg Pgzv Generation Mathematics Learning Standards (jvvru<ll y y 0p{ugf0iqxlewttkewnwo/kpuvtwevkqplpgy/{qtm/state-next-generation-mathematics-learning-standards).

The guide provides educators with pertinent information about the test development process, the learning standards that the tests are designed to measure, the format of the testing sessions which includes what v{rgu qh swguvkqpu ykm dg cumgf. vjg guvk o cvgf cxgtcig ngpivj qh vjg vguvkpi uguukqpu. cpf yjcv o cvjg o cvkeu vqqnu ctg cmqy cdng fwtkpi vguvkpi0 Nkpmu vq cf fkvkqpcn tguqwtegu ctg rtqxkfgf vq hwtvjgt gpjcpeg gfwecvqtuø understanding of the structure of the mathematics tests. Educators are encouraged to review the guide prior to the test administration to gain familiarity with the test format. The information presented can also be used as a platform for educator discussion on how student assessment results can guide future instruction.

The Elementary and Intermediate testing schedule for the spring administration can be found on the Department's <u>website</u> (<u>https://www.nysed.gov/state-assessment/grades-3-8-test-schedules</u>). Questions tgictfkpi vjg Pgy [qtm Uvcvg Vguvkpi Rtqitco cpf vguv fgukip oc{ dg cfftguugf vq vjg Q eg qh Uvcvg Cuuguu ogpv cv <u>emscassessinfo@nysed.gov</u>0 Swguvkqpu tgictfkpi vjg Pgy [qtm Uvcvg Ngctpkpi Uvcpfctfu oc{ dg cfftguugf vq vjg Q eg qh Ewttkewnwo cpf Kpuvtwevkqp cv <u>emscurric@nysed.gov</u>.

Grades 3–8 Mathematics Educator Guide

The Next Generation Mathematics Learning Standards

The Pgy [qtm Uvcvg Pgzv Igpgtcvkqp Ocvjgocvkeu Ngctpkpi Uvcpfctfu fgŁpg vjg mpqyngfig. umknu. cpf understandings that individuals can and do habitually demonstrate over time when exposed to high-quality kpuvtwevkqpcn gpxktqp o gpvu cpf ngctpkpi gzrgtkgpegu0 Vjg Ngctpkpi Uvcpfctfu. fgŁpgf vjtqwij vjg kpvgitcvkqp qh vjg Uvcpfctfu hqt Ocvjgocvkecn Eqpvgpv cpf vjg Uvcpfctfu hqt Ocvjgocvkecn Rtcevkeg. eqnngevkxgn{. ctg hqewugf cpf eqjgukxg ô fgukipgf vq uwrrqtv uvwfgpv ceeguu vq vjg mpqyngfig cpf wpfgtuvcpfkpi qh vjg mathematical concepts that are necessary to function in a world very dependent upon the application of o cvjgocvkeu0 Uvwfgpvu ctg gzrgevgf vq wpfgtuvcpf o cvj eqpegrvwcm{. wug rtqegfwtcn umknu. cpf uqnxg o cvj problems rooted **W**O**h**£

Grades 3-8 Mathematics Educator Guide

Domains, Clusters, Standards, and Sequencing in Instruction and Assessment

The Grades 3–8 Mathematics Tests will measure the NYS Next Generation Mathematics Learning Standards.

Grade 3

Grades 3-8 Mathematics Educator Guide

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Grade 4

Grade 3 Post-Test Standards Assessed in Grade 4

Vjg vcdng dgnqy ujqyu vjg Itcfg 5 rquv/vguv uvcpfctfu vjcv ctg cuuguugf qp vjg Itcfg 6 Pgy [qtm Uvcvg Ocvjgocvkeu Cuuguu ogpv0 Hqt oqtg kphqt ocvkqp cdqwv vjg P [U Pgzv Igpgtcvkqp Ocvjgocvkeu Ngctpkpi Standards Itcfgu 56: Rquv/vguv Uvcpfctfu Fgukipcvkqpu. rngcug tghgt vq vjg ygdukvg (<u>https://www.nysed.gov/</u> curriculum-instruction/next-generation-mathematics-learning-standards-grades-3-8-post-test-recommendations).

Domain	Cluster	Standard(s)
	Population and intermed data	NY-3.MD.3
Measurement	Represent and interpret data.	P [/50O F06
and Data	Geometric measurement: recognize perimeter as an DWWUEWRISD DOGWE between linear and area measures.	NY-3.MD.8a, 8b
Geometry	Reason with shapes and their attributes.	P [/50 I 03

Grades 3–8 Mathematics Educator Guide 32

Grade 4 Post-Test Standards Assessed in Grade 5

Vjg vcdng dgnqy ujqyu vjg Itcfg 6 rquv/vguv uvcpfctfu vjcv ctg cuuguugf qp vjg Itcfg 7 Pgy [qtm Uvcvg Ocvjgocvkeu Cuuguu ogpv0 Hqt oqtg kphqt ocvkqp cdqwv vjg P [U Pgzv Igpgtcvkqp Ocvjgocvkeu Ngctpkpi Standards Itcfgu 56: Rquv/vguv Uvcpfctfu Fgukipcvkqpu. rngcug tghgt vq vjg ygdukvg (<u>https://www.nysed.gov/</u> curriculum-instruction/next-generation-mathematics-learning-standards-grades-3-8-post-test-recommendations).

Domain	Cluster	Standard(s)
Number and		P[/60PH07
Operations— Fractions	Understand decimal notation for fractions, and compare decimal fractions.	P[/60PH08
		P [/60PH09
Measurement	Solve problems involving measurement and	P [/60OF03
and Data	conversion of measurements from a larger unit to a smaller unit.	P [/60OF04c. 4d

Grade 6

Grade 5 Post-Test Standards Assessed in Grade 6

Vjg vcdng dgnqy ujqyu vjg Itcfg 7 rquv/vguv uvcpfctfu vjcv ctg cuuguugf qp vjg Itcfg 8 Pgy [qtm Uvcvg Ocvjgocvkeu Cuuguu ogpv0 Hqt oqtg kphqt ocvkqp cdqwv vjg P [U Pgzv Igpgtcvkqp Ocvjgocvkeu Ngctpkpi Standards Itcfgu 56: Rquv/vguv Uvcpfctfu Fgukipcvkqpu. rngcug tghgt vq vjg ygdukvg (<u>https://www.nysed.gov/</u> curriculum-instruction/next-generation-mathematics-learning-standards-grades-3-8-post-test-recommendations).

Domain	Cluster	Standard(s)
	Write and interpret numerical expressions	P [/70QC03
Operations and Cnigdtcke Vjkpmkpi	write and interpret numerical expressions.	P [/70QC04
	Analyze patterns and relationships.	P [/70QC05
Competers	Graph points on the coordinate plane to solve	P [/70 I 03
Geometry	real-world and mathematical problems.	P [/70 I 04

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Grades 3–8 Mathematics Educator Guide

Domain	Cluster	Standard(s)	Post Standard
The Number			
System			

Grade 7 Post-Test Standards Assessed in Grade 8

Vjg vcdng dgnqy ujqyu vjg Itcfg 9 rquv/vguv uvcpfctfu vjcv ctg cuuguugf qp vjg Itcfg : Pgy [qtm Uvcvg Ocvjgocvkeu Cuuguu ogpv0 Hqt oqtg kphqt ocvkqp cdqwv vjg P [U Pgzv Igpgtcvkqp Ocvjgocvkeu Ngctpkpi Standards Itcfgu 56: Rquv/vguv Uvcpfctfu Fgukipcvkqpu. rngcug tghgt vq vjg ygdukvg (<u>https://www.nysed.gov/</u> curriculum-instruction/next-generation-mathematics-learning-standards-grades-3-8-post-test-recommendations).

Domain	Cluster	Standard(s)
	Draw, construct, and describe geometrical	P [/90 I 04
Geometry	Кроспеткночкихин them.	NY-7.G.3
	Solve real-life and mathematical problems involving angle measure, area, surface area, and volume.	P [/90 I 06
		P [/90 I 07
		NY-7.G.6

Testing Sessions

The Grades 3-8 Mathematics Tests consist of

Test Design

In Grades 3-8, students are required to apply mathematical understandings and mathematical practices

Grades 3–8 Mathematics Educator Guide 42

Test Blueprint

Cm swguvkqpu qp vjg Itcfgu 56: Ocvjgocvkeu Vguvu ogcuwtg vjg Pgzv Igpgtcvkqp Ocvjgocvkeu Ngctpkpi

Domain-Level Test Blueprint—Percent Ranges for Grade 7 Test					
Ratios and					

Question Formats

Vjg I tcfgu 56: Ocvjgocvkeu Vguvu eqpvckp 3/etgfkv ownvkrng/ejqkeg swguvkqpu. 3/etgfkv eqpuvtwevgf/tgurqpug swguvkqpu 4/etgfkv eqpuvtwevgf/tgurqpug swguvkqpu. cpf 5/etgfkv eqpuvtwevgf/tgurqpug swguvkqpu0 Hqt ownvkrng/ choice questions, students select the correct response from four answer choices. For the constructed-response swguvkqpu uvwfgpvu y tkvg cp cpu y gt vq cp qrgp/gpfgf swguvkqp cpf oc{ dg tgswktgf vq ujqy vjgkt y qtm0 kp some cases, they may be required to provide a written explanation for how they arrived at their answers. Uq og vguv swguvkqpu vctigv oqtg vjcp qpg uvcpfctf qt cuuguu cp gpvktg enwuvgt0 Cu uwej. ocp{ kpfkxkfwcn vguv swguvkqpu cuuguu Ugrvg odgt/vq/CrtknlOc{ uvcpfctfu kp eqplwpevkqp ykvj Oc{/vq/Lwpg uvcpfctfu htq o rcuv grades (i.e., post-test standards).

Multiple-Choice Questions

Ownvkrng/ejqkeg swguvkqpu yknn ockpn{ dg wugf vq cuuguu rtqegfwtcn umknnu cpf eqpegrvwcn wpfgtuvcpfkpi0 Ocp{ ownvkrng/ejqkeg swguvkqpu tgswktg uvwfgpvu vq eqorngvg ownvkrng uvgru0 Nkmgykug. uqog qh vjgug swguvkqpu ctg nkpmgf vq oqtg vjcp qpg uvcpfctf. ftcykpi qp vjg uk ownvcpgqwu crrnkecvkqp qh ownvkrng umknnu and concepts. Within answer choices, distractors³ will all be based on plausible missteps.

1-Credit Constructed-Response Questions

3/etgfkv eqpuvtwevgf/tgurqpug swguvkqpu tgswktg uvwfgpvu vq eqorngvg c vcum cpf rtqxkfg qpn{ vjgkt Łpcn cpuygt0 Vjg 3/etgfkv eqpuvtwevgf/tgurqpug swguvkqpu yknn qhvgp tgswktg ownvkrng uvgru. cuuguukpi rtqegfwtcn umknnu. cu ygnn cu eqpegrvwcn wpfgtuvcpfkpi cpf crrnkecvkqp0 Yjkng uvwfgpvu oc{ ujqy jqy vjg{ cttkxgf vq vjgkt Łpcn cpuygt. qpn{ vjg Łpcn cpuygt yknn dg ueqtgf0

2-Credit Constructed-Response Questions

4/etgfkv eqpuvtwevgf/tgurqpug swguvkqpu tgswktg uvwfgpvu vq eqorngvg c vcum cpf ujqy vjgkt yqtm or explain their answer0 Vjg 4/etgfkv eqpuvtwevgf/tgurqpug swguvkqpu yknn qhvgp tgswktg ownvkrng uvgru. vjg crrnkecvkqp qh ownvkrng ocvjgocvkeu umknnu. cpf tgcn/yqtnf crrnkecvkqpu0 Ocp{ qh vjg 4/etgfkv eqpuvtwevgf/tgurqpug

Mathematics Rubrics and Scoring Policies

The Grades 3–8 Mathematics Tests will use the rubrics and scoring policies as shown in this guide.

1 Credit	C 3/etgfkv tgurqpug ku c correct answer to the question which indicates a thorough understanding of mathematical concepts and/or procedures.
0 Credits*	C 2/etgfkv tgurqpug ku kpeqttgev. kttgngxcpv. qt kpeqjgtgpv0

1-Credit Constructed-Response Rubric

* Eqpfkvkqp Eqfg C ku crrnkgf yjgpgxgt c uvwfgpv yjq ku rtgugpv hqt c vguv uguukqp ngcxgu cp gpvktg eqpuvtwevgf/tgurqpug swguvkqp kp vjcv uguukqp eq o rngvgn{ dncpm (pq tgurqpug cvvg o rvgf)0

	C 4/etgfkv tgurqpug kpenwfgu vjg eqttgev uqnwvkqp vq vjg swguvkqp cpf fgoqpuvtcvgu c vjqtqwij wpfgtuvcpfkpi qh vjg ocvjgocvkecn eqpegrvu cpflqt rtqegfwtgu kp vjg vcum0		
	This response		
2 Credits	• kpfkecvgu vjcv vjg uvwfgpv jcu eqorngvgf vjg xÆ	S	

2-Credit Constructed-Response Holistic Rubric

1

3 Credits	

The following scoring policies must be applied while scoring the mathematics tests for all Grades 3–8. The rubrics for the constructed-response questions are designed to provide a systematic, consistent method for awarding credit. Each response must be rated carefully using the teacher's professional judgment cpf mpqyngfig qh ocvjgocvkeu0 Cp{ fktgevkqpu cdqwv ceegrvcdng hqtocvu qh cpuygtu owuv dg hqnnqygf (g0i0. fgek ocn pw odgt. tqwpfkpi. uk ornguv hqto. kp vgtou qh)0 Kh vjg cpuygt hqtocv hqt c swguvkqp ku pqv urgekŁgf. ocvjgocvkecm{ gswkxcngpv uqnwvkqpu ujqwnf dg cyctfgf etgfkv0 Rngcug ugg vjg ueqtkpi ocvgtkcnu hqt hwtvjgt fgvcknu qp ceegrvcdng cpuygt hqt ocvu urgekŁe vq kpfkxkfwcn swguvkqpu0

1-Credit Constructed-Response Mathematics Scoring Policies

- 30 The student is **not** tgswktgf vq ujqy yqtm hqt c 3/etgfkv eqpuvtwevgf/tgurqpug swguvkqp. vjgtghqtg. cp{ yqtm ujqyp yknn **not** dg ueqtgf0 C engctn{ kfgpvkLgf eqttgev tgurqpug ujqwnf uvknn tgegkxg hwnn etgfkv0
- 40 Kh vjg uvwfgpv engctn{ kfgpvkŁgu c eqttgev cpuygt dwv hcknu vq y tkvg vjcv cpuygt kp vjg cpuygt urceg. vjg student should still receive full credit.
- 3. If the student provides one legible response (and one response only), the rater should score the response, even if it has been crossed out.
- 60 If the student has written more than one response but has crossed some out, the rater should score only the response that has **not** been crossed out.
- 70 If the student provides more than one response but does not indicate which response is to be considered the correct response and none have been crossed out, the student shall not receive credit.
- 6. If the student does not provide the answer in the form as directed in the question, the student will not receive credit.
- 7. Kp swguvkqpu tgswktkpi pwodgt ugpvgpegu. vjg pwodgt ugpvgpegu owuv dg y tkvygp jqtk|qpvcm{0
- 8. Yjgp ogcuwtkpi cpingu ykvj c rtqvtcevqt. vjgtg ku c +1/7 fgitggu fgxkcvkqp cnnqygf qh vjg vtwg measure.
- 9. Eqpfkvkqp Eqfg C ku crrnkgf y jgpgxgt c uvwfgpv y jq ku rtgugpv hqt c vguv uguukqp ngcxgu cp gpvktg eqpuvtwevgf/tgurqpug swguvkqp kp vjcv uguukqp eq o rngvgn{ dncpm (pq tgurqpug cvvg o rvgf)0 Vjku ku pqv vq dg eqphwugf ykvj c ueqtg qh |gtq y jgtgkp vjg uvwfgpv fqgu tgurqpf vq rctv qt cm qh vjg swguvkqp. dwv vjcv yqtm tguwnvu kp c ueqtg qh |gtq0

2- and 3-Credit Constructed-Response Mathematics Scoring Policies

30 Kh c uvwfgpv ujqyu vjg yqtm kp qvjgt vjcp c fgukipcvgf õUjqy {qwt yqtmö qt õGzrnckpö ctgc. vjcv yqtm ujqwnf uvkm dg ueqtgf0

40

Mathematics Tools

Why Mathematics Tools?

Reference Sheets

Gcej uvwfgpv vguvkpi kp I tcfgu 76: ykm dg rtqxkfgf ykvj c ocvjgocvkeu tghgtgpeg ujggv hqt vjgkt gzenwukxg wug fwtkpi dqvj Uguukqp 3 cpf Uguukqp 40 Kv ku tgeqo ogpfgf vjcv vjtqwijqwv vjg {gct. vgcejgtu rtqxkfg students opportunities during classroom instruction to gain familiarity with the grade-level reference sheet. **Note:**

Grade 6 Mathematics Reference Sheet

CONVERSIONS

1 yard = 3 fee 1 mile = 5,280 fee 1 cup = 8 fluid ounces 1 pin = 2 cups 1 quar = 2 pin s 1 gallon = 4 quar s 1 li er = 1,000 millili ers

1 pound = 16 ounces 1 on = 2,000 pounds 1 kilogram = 1,000 grams

FORMULAS AND FIGURES

Triangle

CONVERSIONS

1 yard = 3 fee 1 mile = 5,280 fee 1 cup = 8 fluid ounces 1 pin = 2 cups 1 quar = 2 pin s 1 gallon = 4 quar s 1 pound = 16 ounces 1 on = 2,000 pounds

CONVERSIONS ACROSS MEASUREMENT SYSTEMS

1 inch = 2.54 cen ime ers	1 gallon = 3.785 li ers 1 li er = 0.2642 gallon	1 pound = 0.454 kilogram
1 mile = 1.609 kilome ers	r = 0.2042 gallon	r kilografii = 2.2 pounds
1 kilome er = 0.6214 mile		

FORMULAS AND FIGURES

Triangle	General Prism	V = Bh
$A = \frac{1}{2}bh$	1	
Parallelogram		
A = bh		
Trapezoid		
$A = \frac{1}{2}h(b_1 + b_2)$		
Circle r $C = 2\pi r$ $C = \pi d$ $A = \pi r^2$		
Simple Interest I = prt where <i>I</i> is in eres , <i>p</i> is principal, <i>r</i> is ra e, and <i>t</i> is ime		

CONVERSIONS

1 yard = 3 fee 1 mile = 5,280 fee 1 cup = 8 fluid ounces 1 pin = 2 cups 1 quar = 2 pin s 1 gallon = 4 quar s 1 pound = 16 ounces 1 on = 2,000 pounds

CONVERSIONS ACROSS MEASUREMENT SYSTEMS

1 inch = 2.54 cen ime ers 1 me er = 39.37 inches 1 mile = 1.609 kilome ers 10008 pe1.255